



# Operating System Practice

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# Course Roadmap

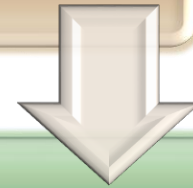
## Advanced Operating System Concepts

- Concepts and Implementation of File System
- Storage Management and I/O Devices
- System Protection and Security



## Exercises on PC and Emulators

- Concepts of the Linux Kernel
- Real-Time System Knowledge
- Android Programming on Android Emulator



## Embedded System Exercises

- Introduction to Embedded System
- Tools and Techniques to Build Embedded Systems
- Implementation on Embedded System Evaluation Boards





# Introduction to Linux

# Advantages of Linux

- ▶ Linux is free, both in source code and cost, due to the GPL
- ▶ Linux is fully customizable in all its components
- ▶ Linux can runs on low-end, inexpensive hardware platforms, e.g., one with 4 MB RAM
- ▶ Linux systems are stable
- ▶ The Linux kernel can be very small and compact
- ▶ Linux is highly compatible with many common applications and functions
- ▶ Linux is well-supported



# Different Type of Operating System Kernels

## ▶ Monolithic kernel

- The entire operating system is working in kernel space
- All parts of the kernel share the same kernel-level memory
- Kernel components might affect other components
- The Linux kernel is an example

## ▶ Microkernel

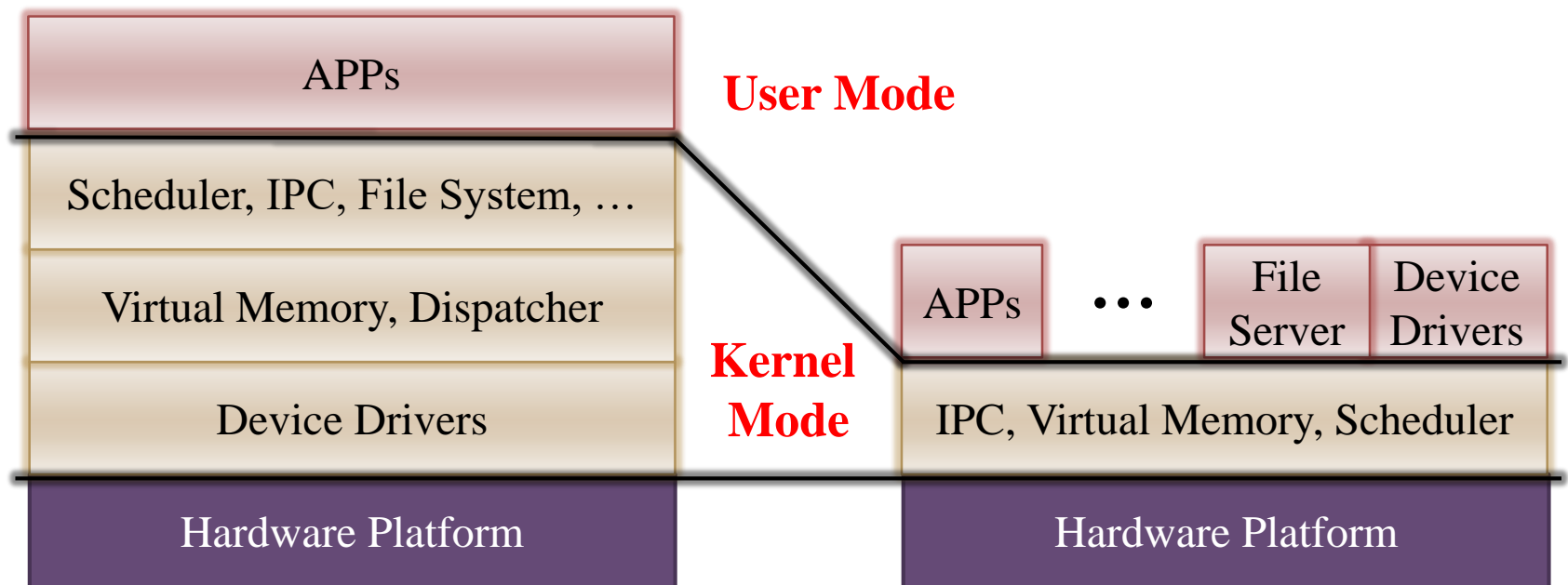
- Kernel functions are partitioned into components
- Communications are via inter process communication (IPC) protocol
- The L4 microkernel is an example



# Monolithic Kernel and Microkernel

## Monolithic Kernel

## Microkernel



# Approaches for Virtualization

- ▶ Virtual Machines on an Host OS
  - For example: VMWare Workstation, Oracle VM VirtualBox
  - Easy to use and install
- ▶ Hypervisors on a Hardware Platform
  - For example: Xen
  - High perform with a very slim software layer
- ▶ Microkernel
  - For example: OKL4 Microkernel
  - Many functions to support the routines of an OS





# History of Linux (1 / 2)

- ▶ 1965: Multiplexed Information and Computing Service (Multics)
  - It is a mainframe timesharing operating system
  - It is developed by Bell Lab, MIT and GE
  - It shows the vision and concept of operating systems
- ▶ 1973: Uniplexed Information and Computing System (UNIX)
  - It has been re-written in C to be portable and quite popular
  - It became closed source in 1979





# History of Linux (2 / 2)

- ▶ 1984: Minix
  - It is on X86 architecture
  - It is originally for education
- ▶ 1991: Linux 0.02
  - It runs on X86
  - It is open source
  - It can be compiled by gcc
  - Everyone can contribute new code to it

*Hello everybody out there using minix- I'm doing a (free) operation system (just a hobby, won't be big and professional like gnu) for 386(486) AT clones.*



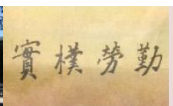
# Features of Linux

- ▶ Monolithic kernel
  - It is large and complex
  - Most commercial Unix variants are monolithic
- ▶ Dynamically linked module
  - It is able to automatically load and unload modules on demand
- ▶ Kernel threading
  - A kernel thread is an execution context that can be independently scheduled
  - Context switches between kernel threads are usually much less expensive than context switches between ordinary processes
- ▶ Multithreaded application support
- ▶ Preemptive kernel
- ▶ Multiprocessor support
- ▶ Filesystem support



# Design Principles

- ▶ Linux is a multiuser, multitasking system with a full set of UNIX-compatible tools
- ▶ Its file system adheres to traditional UNIX semantics, and it fully implements the standard UNIX networking model
- ▶ Main design goals are speed, efficiency, and standardization
- ▶ Linux is designed to be compliant with the relevant POSIX documents



# Kernel Modules

- ▶ Sections of kernel code that can be compiled, loaded, and unloaded independent of the rest of the kernel
- ▶ A kernel module may typically implement a device driver, a file system, or a networking protocol
- ▶ The module interface allows third parties to write and distribute, on their own terms, device drivers or file systems that could not be distributed under the GPL
- ▶ Kernel modules allow a Linux system to be set up with a standard, minimal kernel, without any extra device drivers built in
- ▶ Three components to Linux module support
  - module management
  - driver registration
  - conflict resolution



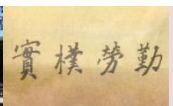
# Module Management

- ▶ Supports loading modules into memory and letting them talk to the rest of the kernel
- ▶ Module loading is split into two separate sections:
  - Managing sections of module code in kernel memory
  - Handling symbols that modules are allowed to reference
- ▶ The module requestor manages currently unloaded modules
  - It also regularly queries the kernel to see whether a dynamically loaded module is still in use
    - Unload a module when it is no longer actively needed



# Driver Registration

- ▶ Allows modules to tell the rest of the kernel that a new driver has become available
- ▶ The kernel maintains dynamic tables of all known drivers, and provides a set of routines to allow drivers to be added to or removed from these tables at any time
- ▶ Registration tables include the following items:
  - Device drivers
  - File systems
  - Network protocols
  - Binary format



# Major and Minor Numbers

- ▶ Major number
  - Each device driver is identified by a unique major number
  - This number is assigned by the Linux Device Registrar
- ▶ Minor number
  - This uniquely identifies a particular instance of a device
  - If there are three devices with the same device driver, they will have the same major number but different minor numbers
- ▶ `mknod [device name][bcp] [Major] [Minor]`
  - b: block devices
  - c: character devices
  - p: a FIFO file





# Process Management

- ▶ Linux process management separates the creation of processes and the running of a new program into two distinct operations
  - The `fork()` system call creates a new process
  - A new program is run after a call to `exec()`
- ▶ A process encompasses all the information that the operating system must maintain to track the context of a single execution of a single program
- ▶ Process properties fall into three groups:
  - Identity
  - Environment
  - Context



# Process Identity

- ▶ Process ID (PID)
  - The unique identifier for the process
  - It is used to specify processes to the operating system when an application makes a system call to signal, modify, or wait for another process
- ▶ Credentials
  - Each process must have an associated user ID and one or more group IDs that determine the process's rights to access system resources and files
- ▶ Namespace
  - Each process is associated with a specific view of the filesystem hierarchy



# Process Environment

- ▶ The process's environment is inherited from its parent
  - The argument vector lists the command-line arguments used to invoke the running program; conventionally starts with the name of the program itself
  - The environment vector is a list of “NAME=VALUE” pairs that associates named environment variables with arbitrary textual values
- ▶ Passing environment variables among processes and inheriting variables by a process's children are flexible
- ▶ The environment-variable mechanism provides a customization of the operating system for each process



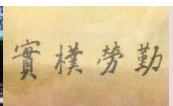
# Process Context

- ▶ The (constantly changing) state of a running program at any point in time
- ▶ The scheduling context is the most important part of the process context; it is the information that the scheduler needs to suspend and restart the process
- ▶ The signal-handler table defines the routine in the process's address space to be called when specific signals arrive
- ▶ The virtual-memory context of a process describes the full contents of the its private address space



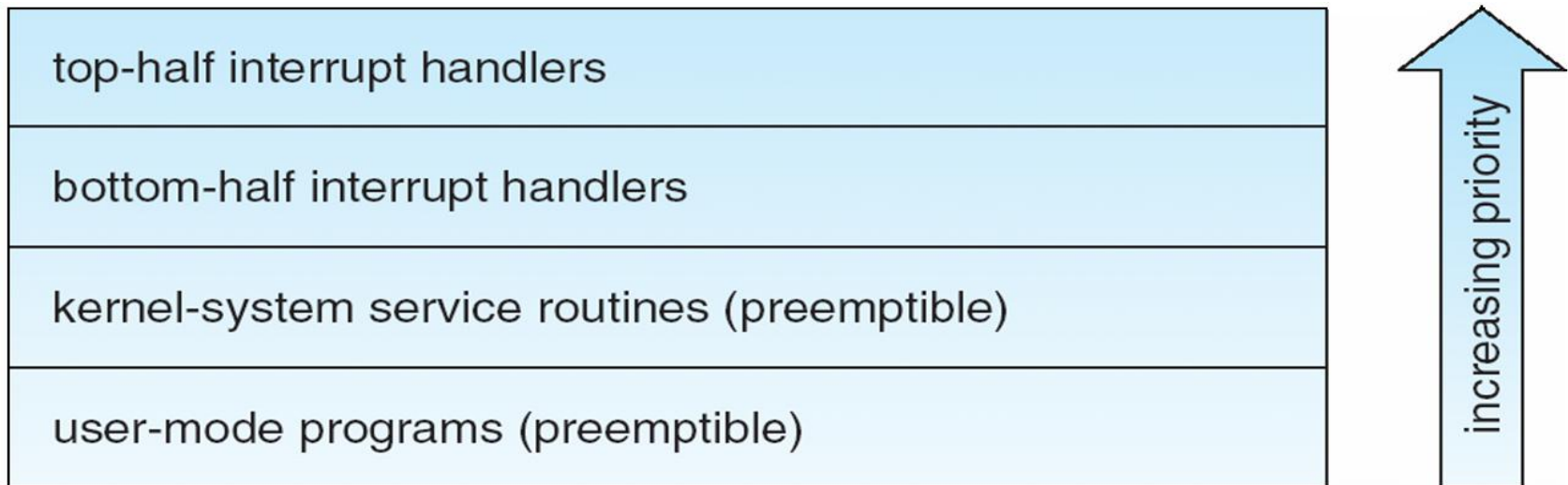
# Kernel Synchronization

- ▶ Kernel synchronization requires a framework that will allow the kernel's critical sections to run without interruption by another critical section
  - Big kernel lock
  - The kernel guarantees that it can proceed without the risk of concurrent access of shared data structures
- ▶ Interrupt service routines are separated into a *top half* and a *bottom half*
  - The top half is a normal interrupt service routine, and runs with recursive interrupts disabled
  - The bottom half runs with all interrupts enabled



# Interrupt Protection Levels

- ▶ Each level may be interrupted by code running at a higher level, but will never be interrupted by code running at the same or a lower level.



# Process Scheduling

- ▶ Linux uses two process-scheduling algorithms
  - A time-sharing algorithm
  - A real-time algorithm for tasks where absolute priorities are more important than fairness
- ▶ For time-sharing processes, Linux uses a prioritized, credit based algorithm
- ▶ Linux implements the FIFO and round-robin real-time scheduling classes





# Executing and Loading User Programs

- ▶ Linux maintains a table of functions for loading programs
  - it gives each function the opportunity to try loading the given file when an exec system call is made
- ▶ The registration of multiple loader routines allows Linux to support both the ELF and a.out binary formats
- ▶ Initially, binary-file pages are mapped into virtual memory
  - Only when a program tries to access a given page will a page fault result in that page being loaded into physical memory
- ▶ An ELF-format binary file consists of a header followed by several page-aligned sections
  - The ELF loader works by reading the header and mapping the sections of the file into separate regions of virtual memory



# Proc File System

- ▶ The proc file system does not store data, rather, its contents are computed on demand according to user file I/O requests
- ▶ When data is read from one of these files, proc collects the appropriate information, formats it into text form and places it into the requesting process's read buffer
- ▶ `cat /proc/cpuinfo` will get the CPU information
  - vendor ID
  - CPU family, CPU cores
  - cache size, TLB size
  - ...





# Real-Time Systems

# An Example of Real-Time Designs

- ▶ A camera periodically takes a photo
- ▶ The image recognition result will be produced before the next period
- ▶ If there is an obstacle, the train automatically brakes

**Time of a Period =  $150/50 = 3\text{s}$**

**Distance of a Period =  $(400 - 100)/2 = 150\text{m}$**

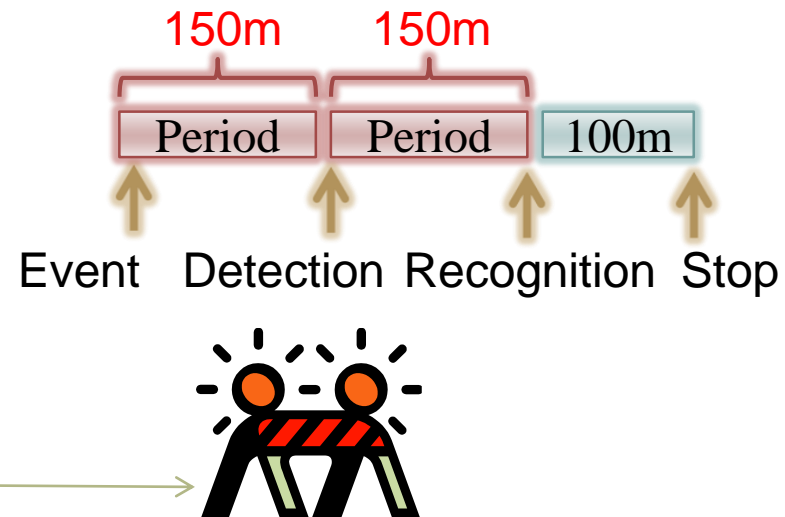
Braking:  $-12.5\text{m/s}^2$

Max Seed:  $50\text{m/s}$

Distance to Stop  
 $25 \times (50/12.5) = 100\text{m}$



Camera Range:  $400\text{m}$

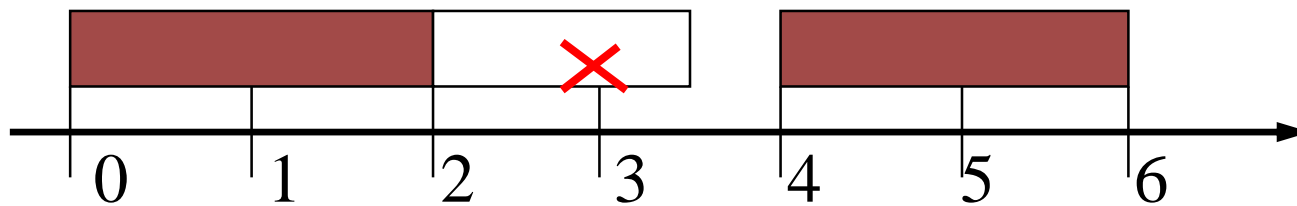


# Multiple Real-Time Tasks

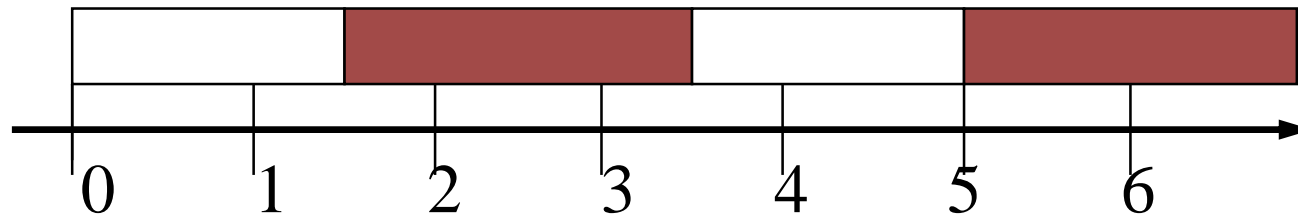
▶ Playing piano: 2 days per 4 days 

Playing chess : 1.5 days per 3 days 

▶ Case 1: Playing piano is always more important



▶ Case 2: Doing whatever is more urgent



# Tentative Assumptions

- ▶ Processes are independent
- ▶ Processes are all periodic
- ▶ The deadline of a request is its next request time
- ▶ A scheduler consists of a priority assignment policy and a priority-driven scheduling mechanism

Reference: C.L. Liu and James. W. Layland, “Scheduling Algorithms for Multiprogramming in a Hard Real-Time Environment,” JACM, Vol. 20, No.1, January 1973, pp. 46-61



# Definitions

- ▶ The **response time** of a request for a process is the time span between the request and the end of the response to that request
- ▶ A **critical instant** of a process is an instant at which a request of that process has the longest response time
- ▶ A **critical interval** for a process is the time interval between the start of a critical instant and the deadline of the corresponding request of the process
  - ➔ A critical instant for any process occurs whenever the process is requested simultaneously with requests for all higher priority processes

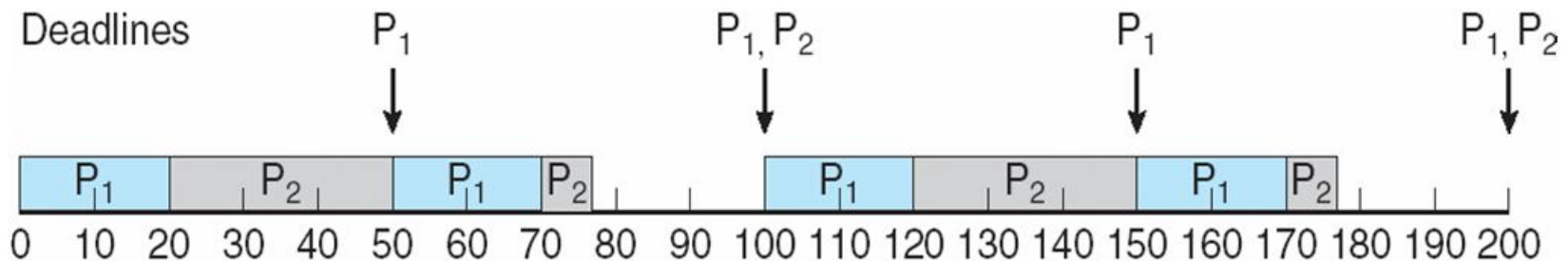
**An observation:** If a process can complete its execution within its critical interval, it is schedulable at all time!





# A Static Scheduling Algorithm— Rate Monotonic Scheduling

- ▶ A static priority is assigned to each task based on the inverse of its period
  - A task with shorter period → higher priority
  - A task with longer period → lower priority
  - For example:
    - $P_1$  has its **period 50** and execution time 20
    - $P_2$  has its **period 100** and execution time 37
    - $P_1$  is assigned a higher priority than  $P_2$

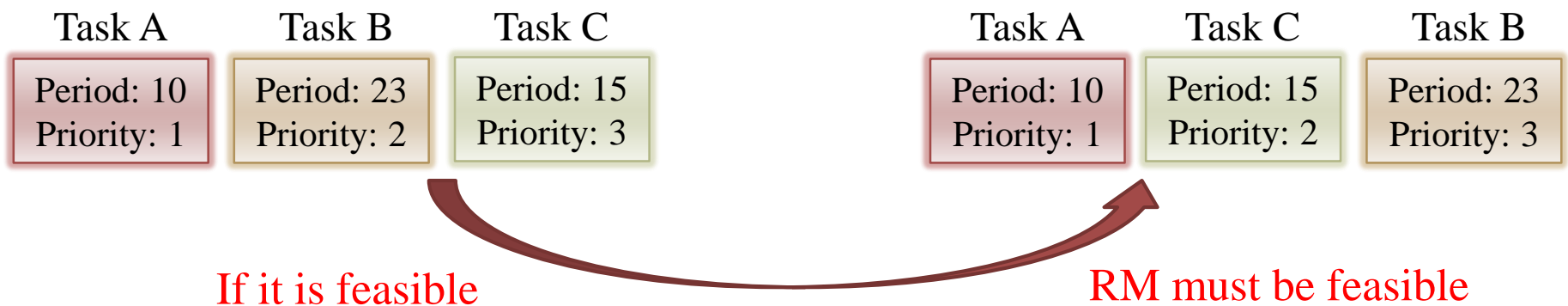


# Property of Rate Monotonic Scheduling

- ▶ The **rate monotonic** (RM) priority assignment assigns processes priorities according to their request rates
  - If a feasible fixed priority assignment exists for some process set, then the rate monotonic priority assignment is feasible for that process set

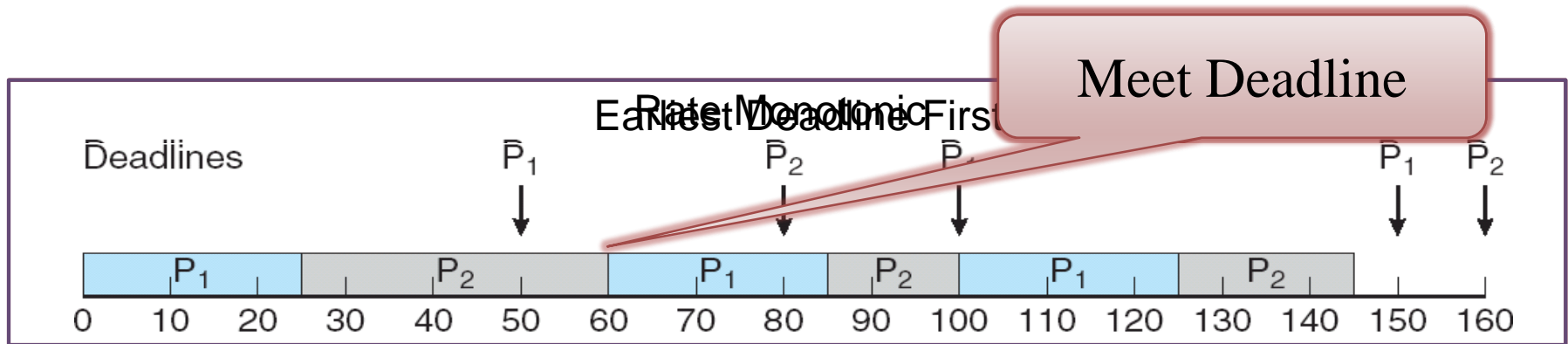
➡ The optimal fixed priority assignment

**Proof.** Exchange the priorities of two tasks if their priorities are out of RMS order.



# A Dynamic Scheduling Algorithm— Earliest Deadline First Scheduling

- ▶ Dynamic priorities are assigned according to deadlines
  - The earlier the deadline, the higher the priority
  - The later the deadline, the lower the priority
  - For example:
    - $P_1$  has its period 50 and execution time 25
    - $P_2$  has its period 80 and execution time 35



# Real-Time Analysis

- ▶ For a task  $\tau_i$  with the period  $P_i$  and the execution time  $C_i$ , the utilization  $U_i$  of  $\tau_i$  is defined as  $U_i = \frac{C_i}{P_i}$
- ▶ For a real-time task set  $T$  the total utilization of the task set is  $\sum_{\tau_i \in T} U_i$
- ▶ If  $\sum_{\tau_i \in T} U_i \leq 69\%$ , Rate Monotonic Scheduling can schedule all tasks in  $T$  to meet all deadlines
  - More precisely, for  $n$  tasks, the  $i$ -th task can meet deadline if

$$\sum_{j=1}^i \frac{C_j}{P_j} \leq i(2^{1/i} - 1)$$

- ▶ If and only if  $\sum_{\tau_i \in T} U_i \leq 100\%$ , Earliest Deadline First Scheduling can schedule all tasks in  $T$  to meet all deadlines

Reference: C.L. Liu and James. W. Layland, "Scheduling Algorithms for Multiprogramming in a Hard Real-Time Environment," JACM, Vol. 20, No.1, January 1973, pp. 46-61

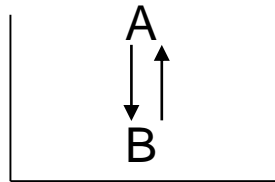


# Scheduling Overheads

## ► Context Switching

- Needed either when a process is preempted by another process, or when a process completes its execution
- Stack Discipline

If process A preempts process B, process A must complete before process B can resume



If it is obeyed, charge the cost of preemption (context switching cost) once to the preempting process!



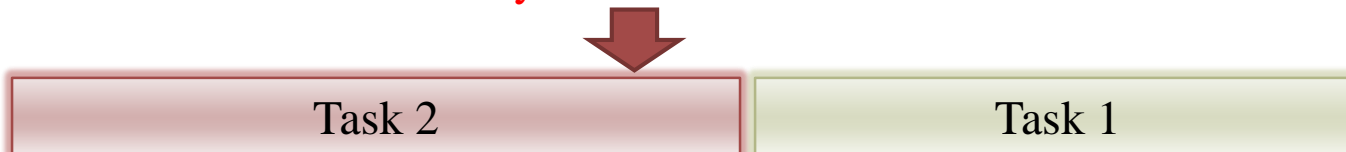
# Least Slack Time Algorithm

- ▶ The least slack time algorithm (LST), which assigns processes priorities inversely proportional to their slack times is also optimal if context switching cost can be ignored
  - The slack time of a process is  $d(t) - t - c(t)$ 
    - $t$ : current time
    - $d(t)$ : deadline
    - $c(t)$ : remaining execution time
  - An example
    - The time  $t = 0$ , two task have the same deadline 20
    - Task 1 has  $c(t) = 7$ , and task 2 has  $c(t) = 8$

$t_1 \rightarrow 13$     $t_1 \rightarrow 11$     $t_1 \rightarrow 11$     $t_1 \rightarrow 9$   
 $t_2 \rightarrow 12$     $t_2 \rightarrow 12$     $t_2 \rightarrow 10$     $t_2 \rightarrow 10$



So many context switches!





# Process Synchronization



# Basic Concept

- ▶ Processes might share non-preemptible resources or have precedence constraints
- ▶ Papers for discussion:
  - L. Sha, R. Rajkumar, J.P. Lehoczky, “Priority Inheritance Protocols: An Approach to Real-Time Synchronization,” IEEE Transactions on Computers, 1990.
  - A.K. Mok, “The Design of Real-Time Programming Systems Based on Process Models,” IEEE Real-Time Systems Symposium, Dec 1994.



# Process Synchronization

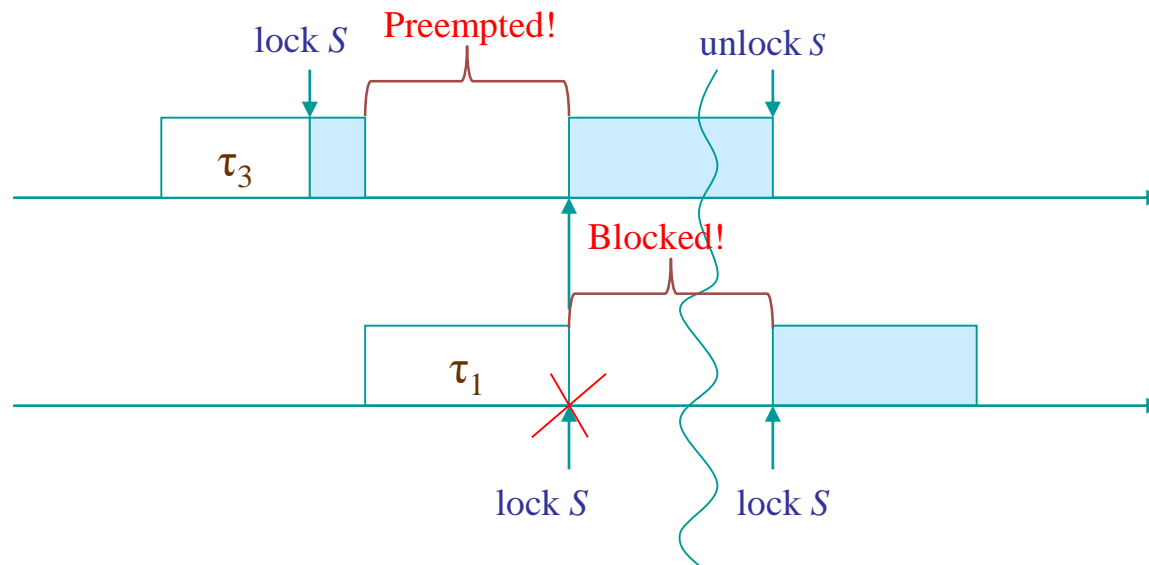
## ► Motivation

- Can we find an efficient way to analyze the schedulability of a process set (systematically)
- What kinds of restrictions on the use of communication primitives are needed so as to efficiently solve the restricted scheduling problem
- How can we control the priority inversion problem
- The lengths of critical sections might be quite different



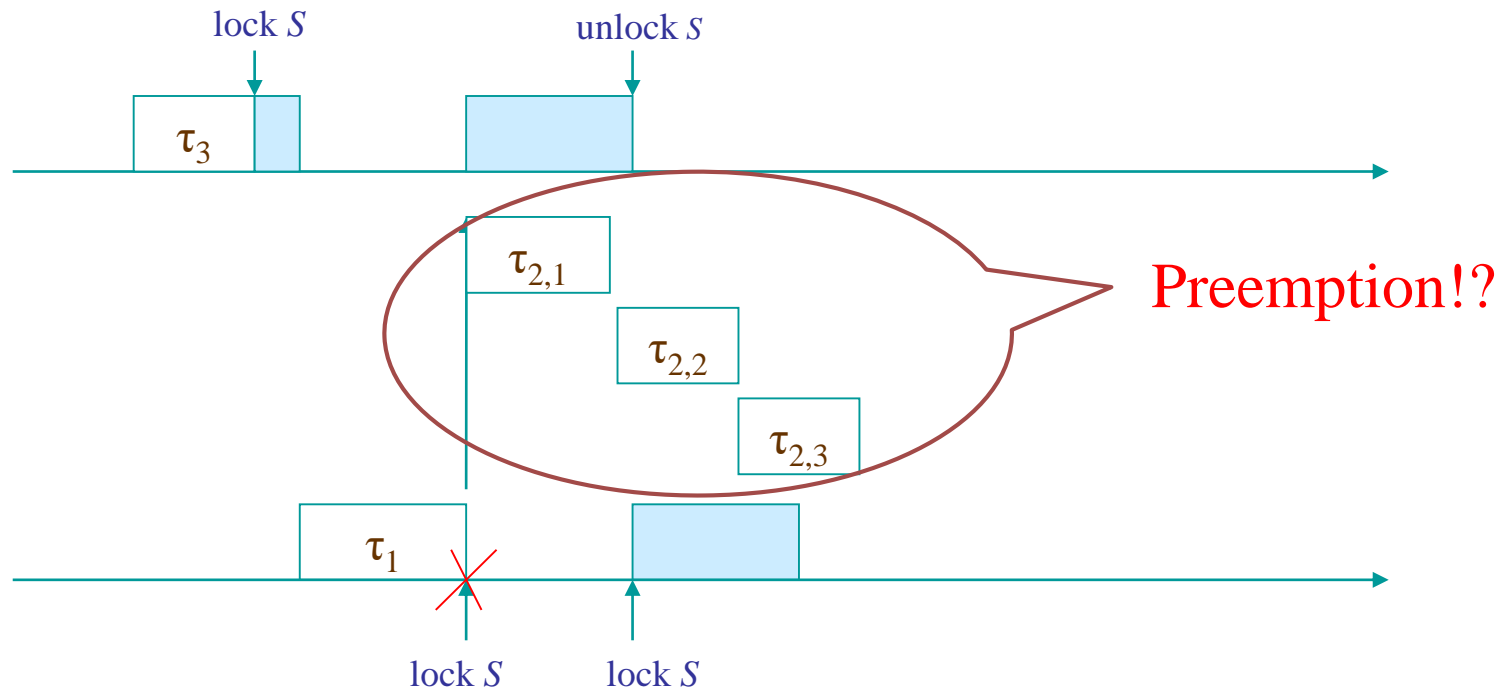
# Blocking and Preemption

- ▶ Blocking: a higher-priority process is forced to wait for the execution of a lower-priority process
- ▶ Preemption: a low-priority process is forced to wait for the execution of a high-priority process



# Priority Inversion

- ▶ When there are a lot of tasks having priority between that of  $\tau_1$  and  $\tau_3$ , there are a lot of priority inversions



# Priority Inheritance Protocol (PIP)

## ▶ Priority-Driven Scheduling

- The process which has the highest priority among the ready processes is assigned the processor

## ▶ Synchronization

- Process  $\tau_i$  must obtain the lock on the semaphore guarding a critical section before  $\tau_i$  enters the critical section
- If  $\tau_i$  obtains the required lock,  $\tau_i$  enters the corresponding critical section; otherwise,  $\tau_i$  is blocked and said to be blocked by the process holds the lock on the corresponding semaphore
- Once  $\tau_i$  exits a critical section,  $\tau_i$  unlocks the corresponding semaphore and makes its blocked processes ready

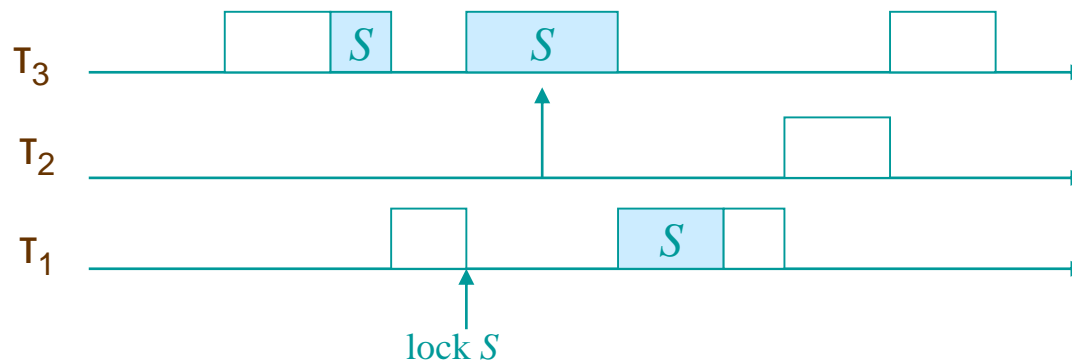
## ▶ Priority Inheritance

- If a process  $\tau_i$  blocks higher priority processes,  $\tau_i$  inherits the highest priority of the process blocked by  $\tau_i$
- Priority inheritance is transitive



# Properties of PIP

- ▶ No priority inversion

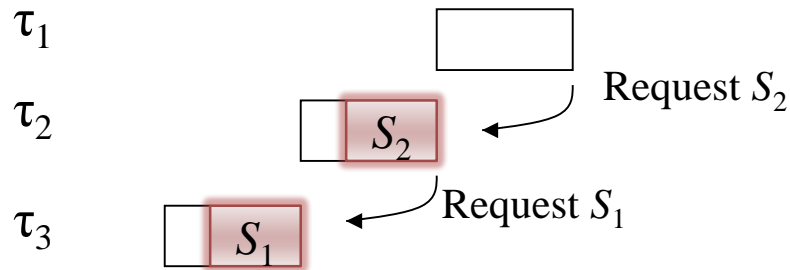


- ▶ A semaphore  $S$  can be used to cause inheritance blocking to task  $J$  only if  $S$  is accessed by a task which has a priority lower than that of  $J$  and might be accessed by a task which has a priority equal to or higher than that of  $J$ .

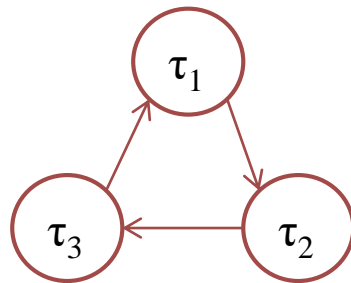


# Concerns of PIP

- ▶ A chain of blocking is possible



- ▶ A deadlock can be formed



# Priority Ceiling Protocol (PCP)

- ▶ The priority ceiling of a semaphore is the priority of the highest priority task that may lock the semaphore
- ▶ The Basic Priority Inheritance Protocol + Priority Ceiling
- ▶ A task  $J$  may successfully lock a semaphore  $S$  if  $S$  is available, and the priority of  $J$  is higher than the highest priority ceiling of all semaphores currently locked by tasks other than  $J$
- ▶ Priority inheritance is transitive





# Properties of PCP

- ▶ The priority ceiling protocol prevents transitive blockings
- ▶ The Priority ceiling Protocol prevents deadlock
- ▶ No job can be blocked for more than one critical section of any lower priority job
- ▶ A set of  $n$  periodic tasks under the **priority ceiling protocol** can be scheduled by the **rate monotonic algorithm** if the following conditions are satisfied:

$$\forall i, \quad 1 \leq i \leq n, \quad \sum_{j=1}^{i-1} \frac{c_j}{p_j} + \frac{c_i + B_i}{p_i} \leq i(2^{1/i} - 1)$$

where  $B_i$  is the worst-case blocking time for  $\tau_i$



# Example of PCP

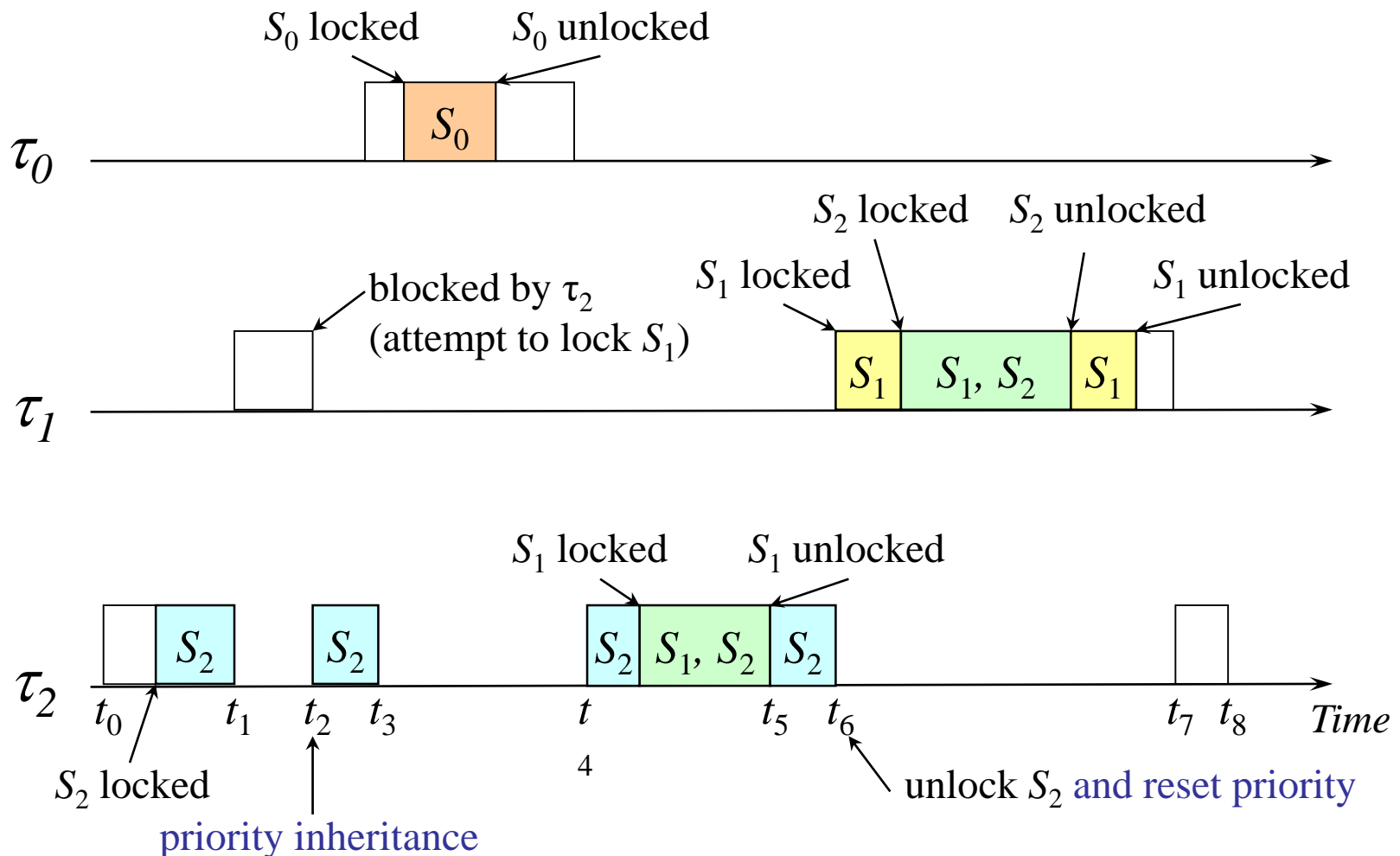
- ▶ Consider 4 tasks,  $t_1$ ,  $t_2$ ,  $t_3$ , and  $t_4$  which have priorities  $x_1$ ,  $x_2$ ,  $x_3$ , and  $x_4$ , respectively, and assume  $x_1 > x_2 > x_3 > x_4$  ( $x_1$  is the highest priority). After we profile the programs of the 4 tasks, we have the following information:
  - Task  $t_1$  will lock semaphore  $S_1$  for 3ms.
  - Task  $t_2$  will lock semaphore  $S_2$  for 10ms and lock semaphore  $S_1$  for 13ms.
  - Task  $t_3$  will lock semaphore  $S_2$  for 8ms and lock semaphore  $S_3$  for 15ms.
  - Task  $t_4$  will lock semaphore  $S_1$  for 15ms and lock semaphore  $S_3$  for 23ms.
  - Please derive the priority ceiling of each semaphore. If priority ceiling protocol is used to manage the semaphore locking, please derive the worst-case blocking time of each task.

Answer: Priority ceilings:  $S_1 \rightarrow x_1$ ,  $S_2 \rightarrow x_2$ ,  $S_3 \rightarrow x_3$ .

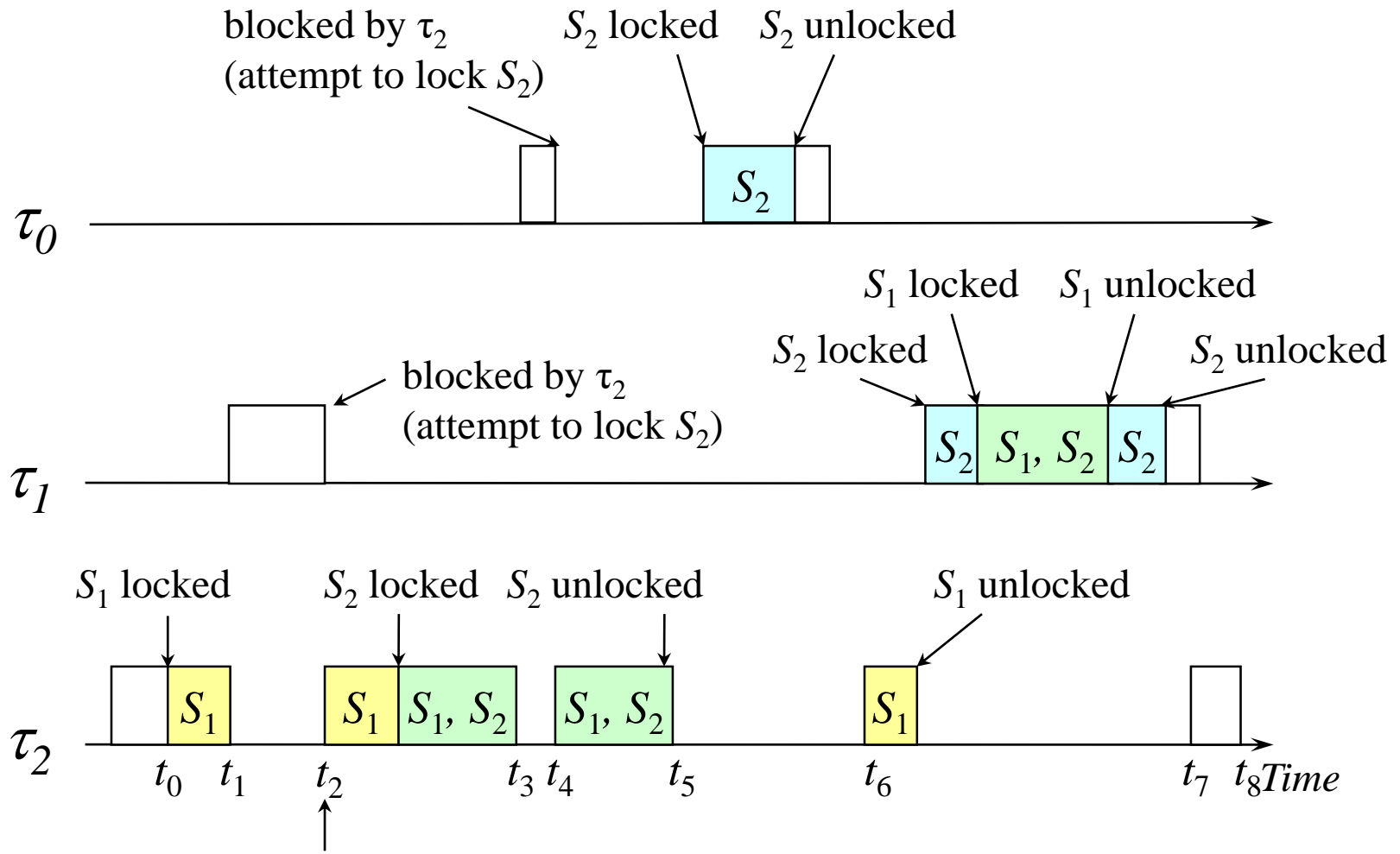
Worst-case blocking times:  $t_1 \rightarrow 15\text{ms}$ ,  $t_2 \rightarrow 15\text{ms}$ ,  $t_3 \rightarrow 23\text{ms}$ ,  $t_4 \rightarrow 0\text{ms}$ .



# Example: Deadlock Avoidance



# Example: Chain Blocking Avoidance



Avoidance blocking occurs!



# Rate Monotonic Analysis

# Periodic Requirements (1 / 2)

Task  $\tau_1$ :  $C_1=20$ ,  $P_1=100$ ,  $U_1=0.2$

Task  $\tau_2$ :  $C_2=40$ ,  $P_2=150$ ,  $U_2=0.267$

Task  $\tau_3$ :  $C_3=100$ ,  $P_3=350$ ,  $U_3=0.286$

- ▶ Total utilization:  $75.3\% \leq 3(2^{\frac{1}{3}} - 1) = 77.9\%$
- ▶ 24.7% of the CPU is usable for lower-priority background computation



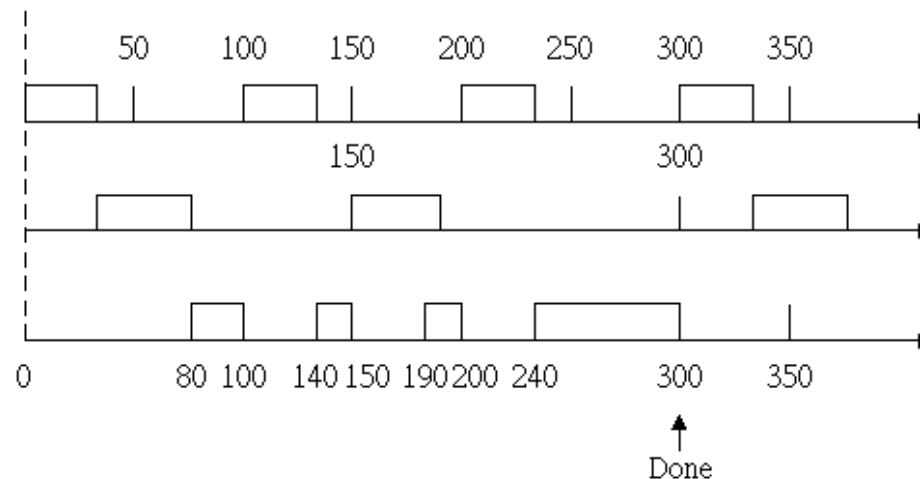
# Periodic Requirements (2 / 2)

Task  $\tau_1$ :  $C_1=40$ ,  $P_1=100$ ,  $U_1=0.4$

Task  $\tau_2$ :  $C_2=40$ ,  $P_2=150$ ,  $U_2=0.267$

Task  $\tau_3$ :  $C_3=100$ ,  $P_3=350$ ,  $U_3=0.286$

- ▶ The utilization of the first two tasks:  $66.7\% \leq 2(2^{\frac{1}{2}} - 1) = 82.8\%$
- ▶ The total utilization:  $95.3\% > 3(2^{\frac{1}{3}} - 1) = 77.9\%$



# Rate Monotonic Analysis (RMA)

## ► A RMA Example:

- $\tau_1(20,100)$ ,  $\tau_2(30,150)$ ,  $\tau_3(80, 210)$ ,  $\tau_4(100,400)$

- $\tau_1$

- $c_1 \leq 100$

- $\tau_2$

- $c_1 + c_2 \leq 100$  or

- $2c_1 + c_2 \leq 150$

- $\tau_3$

- $c_1 + c_2 + c_3 \leq 100$  or

- $2c_1 + c_2 + c_3 \leq 150$  or

- $2c_1 + 2c_2 + c_3 \leq 200$  or

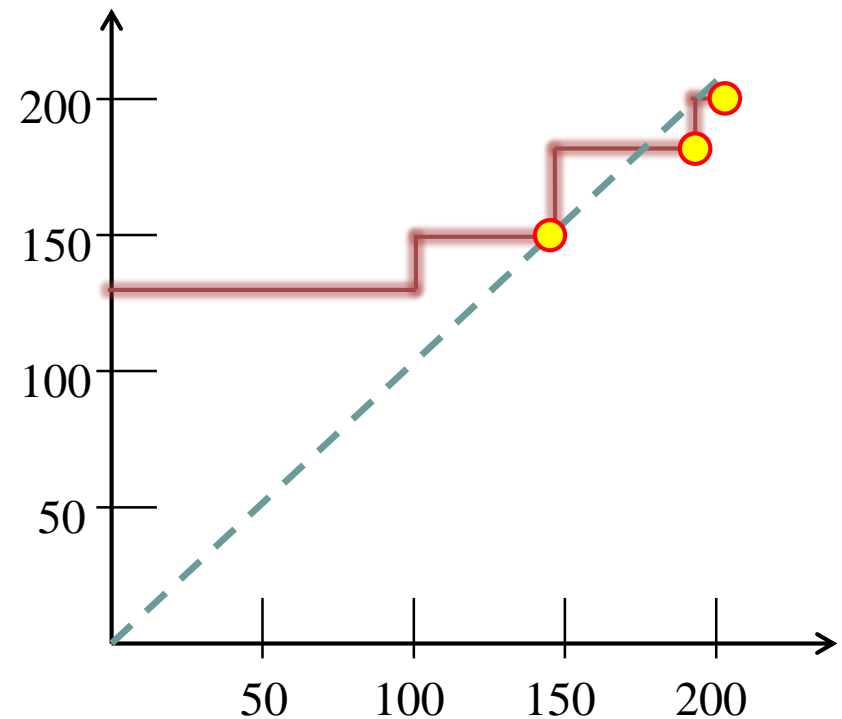
- $3c_1 + 2c_2 + c_3 \leq 210$

- $\tau_4$

- $c_1 + c_2 + c_3 + c_4 \leq 100$  or

- $2c_1 + c_2 + c_3 + c_4 \leq 150$  or

- ...





# RMA with Blocking Consideration (1 / 2)

- ▶ A RMA Example with blocking time:
  - $\tau_1(20,100)$ ,  $\tau_2(30,150)$ ,  $\tau_3(80, 210)$ ,  $\tau_4(100,400)$
  - $\tau_1$ : ( $S_1$ , 5)
  - $\tau_2$ : ( $S_2$ , 15)
  - $\tau_3$ : ( $S_1$ , 10), ( $S_3$ , 5)
  - $\tau_4$ : ( $S_2$ , 5), ( $S_3$ , 20)
- ▶ What is the priority ceiling of each semaphore?
  - $S_1$ :  $\tau_1$ ,  $S_2$ :  $\tau_2$ ,  $S_3$ :  $\tau_3$
- ▶ When PCP is adopted (block once), what is the blocking time of each task?
  - $\tau_1$ : 10,  $\tau_2$ : 10,  $\tau_3$ : 20,  $\tau_4$ : 0



# RMA with Blocking Consideration (2/2)

- ▶ A RMA Example with blocking time:
  - For each task, we have to consider the execution time, period, and blocking time
  - $\tau_1(20,100,10)$ ,  $\tau_2(30,150,10)$ ,  $\tau_3(80, 210,20)$ ,  $\tau_4(100,400,0)$
  - $\tau_1$ 
    - $b_1 + c_1 \leq 100$
  - $\tau_2$ 
    - $b_2 + c_1 + c_2 \leq 100$  or
    - $b_2 + 2c_1 + c_2 \leq 150$
  - $\tau_3$ 
    - $b_3 + c_1 + c_2 + c_3 \leq 100$  or
    - $b_3 + 2c_1 + c_2 + c_3 \leq 150$  or
    - $b_3 + 2c_1 + 2c_2 + c_3 \leq 200$  or
    - $b_3 + 3c_1 + 2c_2 + c_3 \leq 210$
  - $\tau_4$ 
    - ...





# Aperiodic Servers

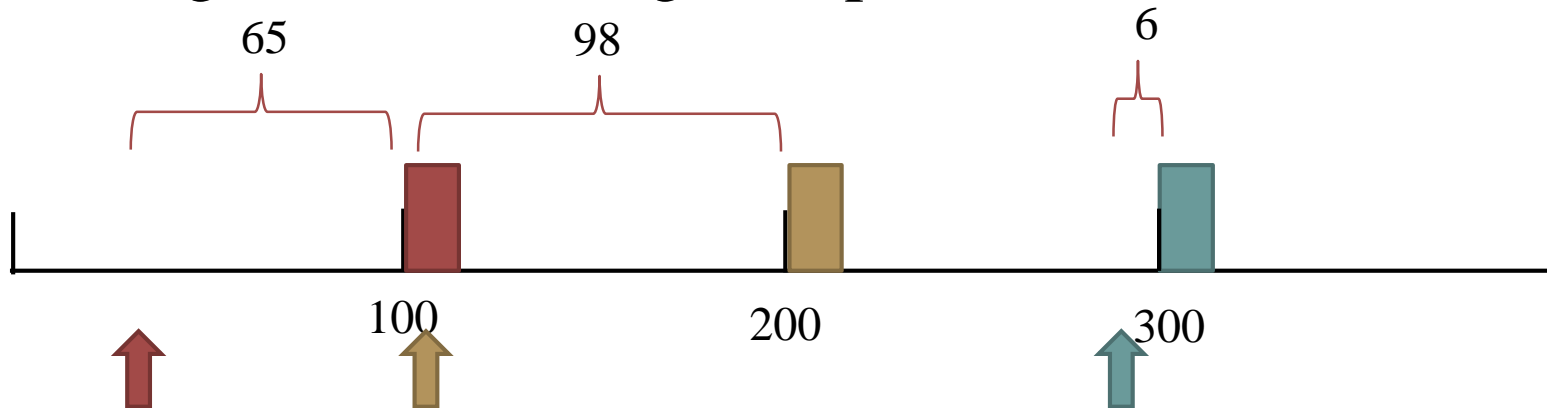
# Observation of Aperiodic Tasks

- ▶ Aperiodic tasks run at irregular intervals
- ▶ Aperiodic deadlines
  - Hard deadline: minimum inter-arrival time
  - Soft deadline: best average response time
- ▶ Services such as
  - User requests
  - Device interrupts
  - ...

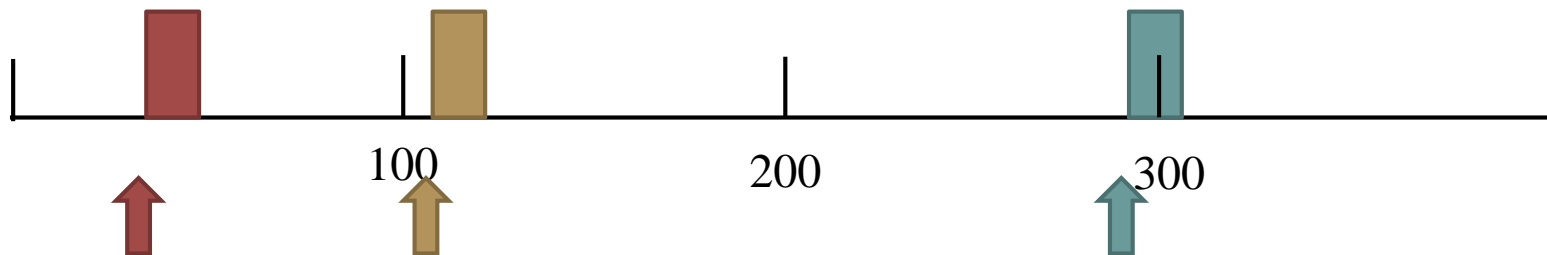


# Scheduling Aperiodic Tasks

- ▶ Polling Server ~ Average Response Time = 50 units

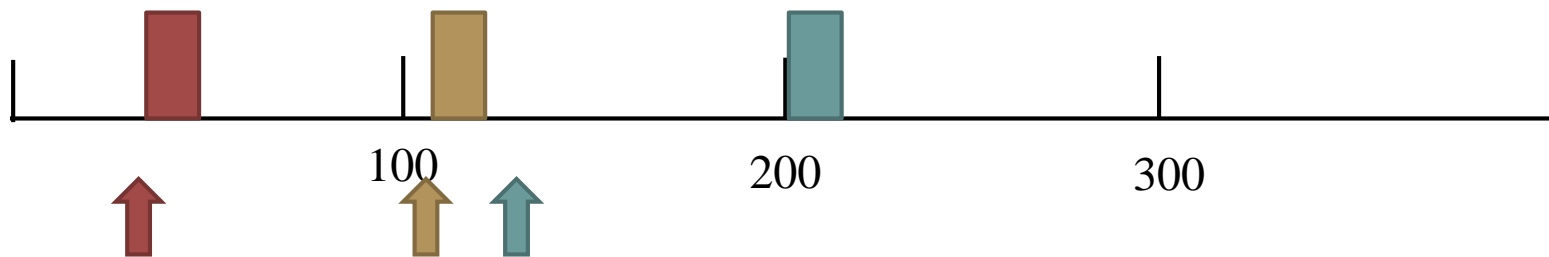


- ▶ Interrupt Server ~ Average Response Time = 1 unit



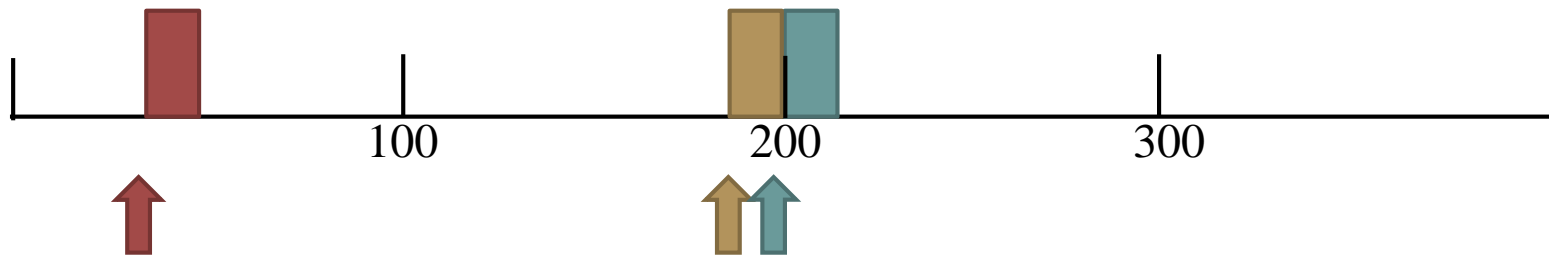
# Deferrable Server

- ▶ Polling Server: the average response time is long
- ▶ Interrupt Server: the computing time of aperiodic tasks is difficult to limited
- ▶ Deferrable Server
  - In each period, a deferrable server has a execution budget
  - When execution budget is used up, server execution drops to a lower (background) priority



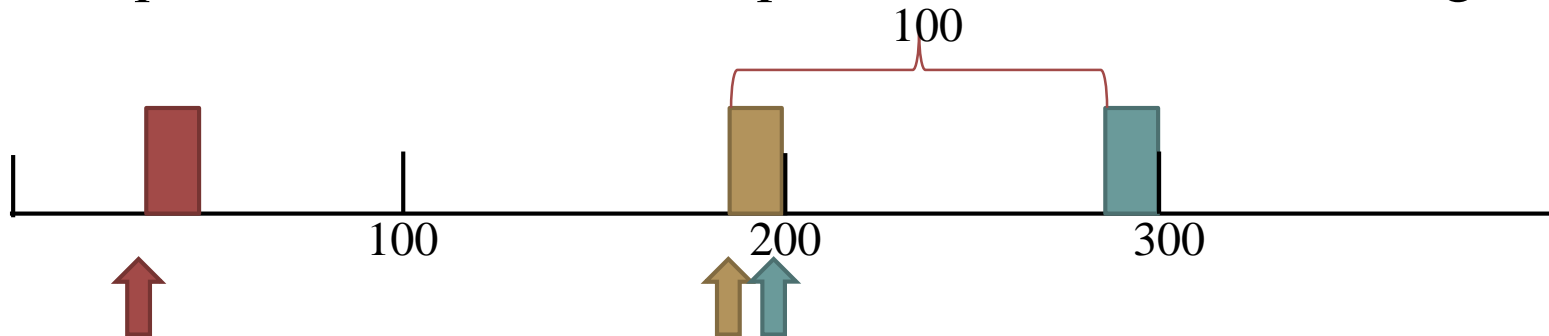
# Sporadic Server

- ▶ Deferrable Server might consume two times of the execution budget in short time



- ▶ Sporadic Server

- Replenishment occurs one “period” after the start of usage



# Properties of Sporadic Server

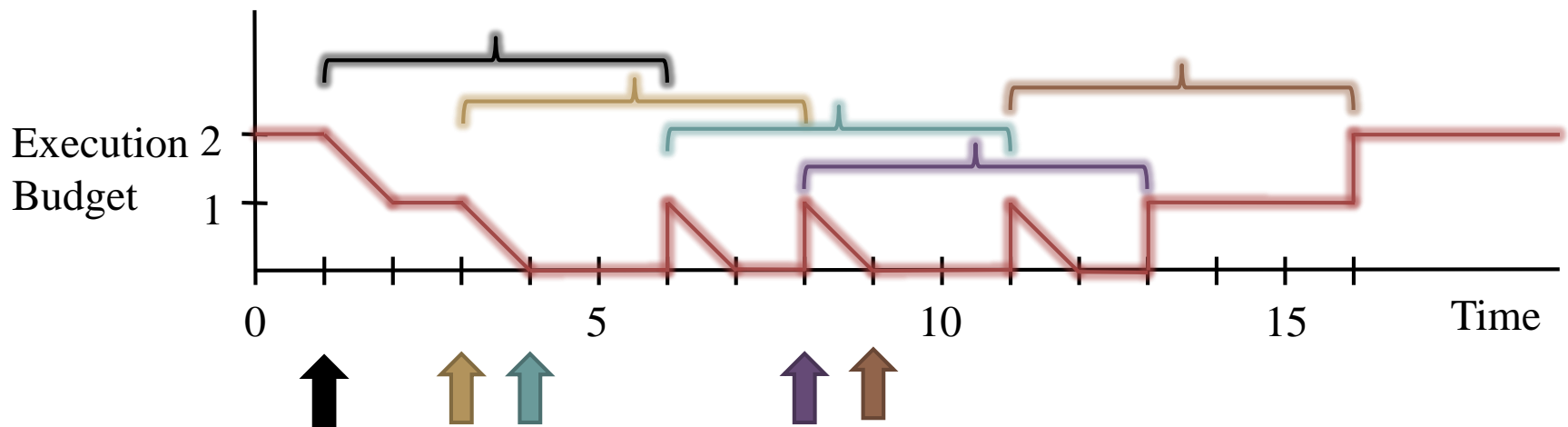
- ▶ A sporadic server differs from a deferrable server in its replenishment policy:
  - A 100 ms deferrable server replenishes its execution budget every 100 ms, no matter when the execution budget is used
  - The affect of a sporadic server on lower priority tasks is no worse than a periodic task with the same period and execution time





# An Example of Sporadic Server

- ▶ A sporadic server has a replenishment period 5 and an execution budget 2
- ▶ Each event consumes the execution 1
- ▶ Events arrive at 1, 3, 4, 8, 9



# Properties of Sporadic Server

- ▶ For a sporadic server has a replenishment period  $X$  and an execution budget  $Y$ 
  - Given a set of sporadic tasks, If
    - Each of the aperiodic tasks has its minimum inter-arrival time no less than  $X$
    - The total execution of the task set is no more than  $Y$
  - All sporadic tasks can meet the deadline constraints
- ▶ When a system consists of periodic tasks and sporadic servers
  - A sporadic server with replenishment period  $X$  and an execution budget  $Y$  can be consider as a periodic task with a period  $X$  and an execution time  $Y$
  - The system can then use analysis scheme of RM or EDF

